Fermi National Accelerator Laboratory

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A Determination of $\sin\theta^2$ from the Forward-Backward Asymmetry in $p\bar{p} \Rightarrow Z^0X \Rightarrow e^+e^-X$ Interactions at $\sqrt{\delta} = 1.8$ TeV.

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Abstract

An analysis of the forward–backward asymmetry in Z^0 decays using data from the Collider Detector at Fermilab at $\sqrt{s} = 1.8$ TeV yields $A_{\rm FB} = (5.3 \pm 5.9(\text{stat}) \pm 0.4(\text{sys}))\%$ and $\sin^2\bar{\theta}_W = 0.228^{+0.017}_{-0.015}(\text{stat}) \pm 0.002(\text{sys})$.

In the Standard Model [1], the neutral current can be defined by a mixture of weak and electromagnetic currents with mixing angle $\bar{\theta}_W$:

$$J_\mu^{NC} = J_\mu^{I_3} - \sin^2\bar{\theta}_W J_\mu^{EM}. \tag{1}$$

The weak component of the neutral current violates parity, and leads to a charge asymmetry in the decay angular distribution of the Z^0. This asymmetry depends on the relative magnitudes of the weak and electromagnetic components of the neutral current, and hence on $\sin^2\bar{\theta}_W$. In this paper we present a measurement of the forward–backward asymmetry in $p\bar{p} \to Z^0 X \to e^+e^- X$ events, which probes the neutral current coupling to light quarks at the Z^0 mass scale, and leads to a measurement of $\sin^2\bar{\theta}_W$

In hadronic collisions, direct e^+e^- pairs are produced by the annihilation of a quark–antiquark ($q\bar{q}$) pair via either a photon or Z^0. The angular distribution for $p\bar{p} \to Z^0 X \to$

e^+e^-X is expected to be asymmetric in $\cos\hat{\theta}$, where $\hat{\theta}$ is defined to be the angle between the outgoing e^+ and incoming $\bar{q}$ in the rest frame of the e^+e^- pair. The forward-backward asymmetry is defined by

$$A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B}, \tag{2}$$

where $\sigma_F = \int_0^1 [d\sigma/d(\cos\hat{\theta})]\, d(\cos\hat{\theta})$ and $\sigma_B = \int_{-1}^0 [d\sigma/d(\cos\hat{\theta})]\, d(\cos\hat{\theta})$. The lowest order cross section has the form [2] $d\sigma/d(\cos\hat{\theta}) = A(1+\cos^2\hat{\theta}) + B\cos\hat{\theta}$ and has contributions from photon exchange, Z^0 exchange, and photon–Z^0 interference. The dominant contribution to $A_{\rm FB}$ near the Z^0 resonance comes from Z^0 exchange.

We present a measurement of $A_{\rm FB}$ and $\sin^2\bar{\theta}_W$ using data corresponding to an integrated luminosity of 4.1 $\rm pb^{-1}$ from $p\bar{p}$ collisions at $\sqrt{s} = 1.8$ TeV collected with the Collider Detector at Fermilab (CDF). The CDF detector is described in detail elsewhere [3]. Briefly, scintillator hodoscopes (BBC) located on either side of the detector identify inelastic events. Time–projection chambers (VTPC) measure the position of the event vertex. A drift chamber surrounds the VTPC and measures the momentum of charged particles in a 1.4 Tesla solenoidal magnetic field. Electromagnetic and hadronic calorimeters extend from $-4.2 < \eta < 4.2$ in a projective tower geometry, where $\eta \equiv -\ln[\tan(\theta/2)]$ [4]. A proportional chamber near shower maximum in the central ($|\eta| < 1.1$) electromagnetic calorimeter measures shower shape and position.

The trigger requires a central electromagnetic cluster with (i) transverse energy $E_T > 12$ GeV ($E_T = E\sin\theta$), (ii) an associated track with transverse momentum > 6 GeV, and (iii) the ratio of hadronic to electromagnetic E_T in the cluster $(HAD/EM) < 12.5\%$.

We require each Z^0 event to have one electron in the central region, where there is good momentum determination, so that the charge of at least one electron and the sign of $\cos\hat{\theta}$ can be determined, and a second electron with $|\eta| < 3.5$. Both electron clusters must be located away from calorimeter edges so that their energies are well measured. The event vertex is required to be within 60 cm in the z direction of the nominal interaction point.

One central electron is required to have (i) $E_T > 15$ GeV and lateral energy sharing in the

calorimeter towers consistent with an electron shower, (ii) the ratio of cluster energy to track momentum $E/P < 1.5$, (iii) a shower in the strip chambers with a profile consistent with an electron shower and centroid position within 1.5 cm in the ϕ direction and 3.0 cm in the z direction of the extrapolated track, and (iv) isolation $I < 0.1$, where $I = (E_C - E_T)/E_C$, E_C being the total transverse energy in a cone in η-ϕ space of radius 0.4 centered on the cluster.

The second electron is required to have (i) $E_T > 15$ GeV, (ii) $I < 0.1$, (iii) if in the central region, $E/P < 1.5$, (iv) if in the plug region, $HAD/EM < 0.05$, transverse energy profile consistent with test beam electrons, and a track in the VTPC, (v) if in the forward region, $HAD/EM < 0.05$ and longitudinal energy profile consistent with test beam electrons.

We take as our Z^0 sample the 252 events with $75 < M_{ee} < 105$ GeV. The background from QCD processes is estimated from studies of isolation to be 7 ± 3 events. If this background is symmetric in $\cos\hat{\theta}$, the observed asymmetry is reduced by 3% of itself. The background from τ pairs is estimated from Monte Carlo to be less than 0.5 events. The background from $W + \text{jet} \rightarrow e\nu + \text{jet}$ in which the jet fakes a second electron is estimated to be less than 0.4 events.

Due to QCD processes, Z^0's are produced with momentum transverse to the beam direction, p_T^Z. In this case, the p and $\bar{p}$ are not collinear in the e^+e^- rest frame, and the quark directions are not the p or $\bar{p}$ directions. We adopt the method of Collins and Soper [5] in which $\cos\hat{\theta}$ is measured with respect to the average of the p and $-\bar{p}$ directions in the e^+e^- rest frame. This introduces a small, p_T^Z dependent smearing of the measured angular distribution. In this method, we assume all quarks are valence quarks, *i.e.* the q comes from the p and the $\bar{q}$ from the $\bar{p}$. The small contribution in which the $\bar{q}$ comes from the p (approximately 10% of the cross section) gives an asymmetry opposite to that from the valence quarks. This contribution is included in our calculation of $\sin^2\bar{\theta}_W$ below.

The angular distribution $dn/d\cos\hat{\theta}$ is plotted before acceptance corrections in Figure 1a. It has the predicted parabolic shape except at large $|\cos\hat{\theta}|$ where the electron E_T cut

	ΔA_{FB}	σA_{FB}	$\Delta \sin^2\bar{\theta}_W$	$\sigma \sin^2\bar{\theta}_W$
QCD Background	+0.14%	0.06%	-0.0004	0.0002
$\ln \mathcal{L}$ fitter	0%	0.26%	0.0	0.0008
Electron Trigger	0%	0.23%	0.0	0.0006
Track Reconstruction	0%	0.19%	0.0	0.0005
Electron Selection	0%	0.10%	0.0	0.0003
Energy Scale	0%	0.03%	0.0	0.0001
p_T^Z spectrum	+0.14%	0.09%	-0.0004	0.0003
QED Corrections	-	-	-0.0014	0.0014
Weak Corrections	-	-	-0.0013	0.0002
Parton Distribution	-	-	-	0.0004

Table 1: Corrections and systematic uncertainties for A_{FB} and $\sin^2\bar{\theta}_W$

reduces the acceptance. Figure 1b shows a plot of $(1/\sigma)d\sigma/d\cos\hat{\theta}$ corrected bin-by-bin for acceptance, using the ISAJET [6] Monte Carlo and a simple detector simulation.

We use a log likelihood fit to determine $A_{\rm FB}$; the result does not depend on the angular dependence of the acceptance, provided the acceptance is symmetric with respect to $\cos\hat{\theta}$. The fit yields $A_{FB} = (5.0 \pm 5.9)\%$, and is shown in Figure 1b. The photon–Z^0 interference term contributes an asymmetry of approximately 1.5% in our mass region. Using $A_{\rm FB}$ and the lowest order cross section with MRSB [7] parton distribution functions we derive the lowest order value $\sin^2\bar{\theta}_W|_{lo} = 0.231^{+0.017}_{-0.015}(\text{stat})$ [8].

Systematic uncertainties on $A_{\rm FB}$ and $\sin^2\bar{\theta}_W$ come from several sources and are summarized in Table 1. Bias in the fitting procedure is determined to be less than 0.26% by fitting many Monte Carlo data samples. Systematic uncertainties due to trigger, track reconstruction, and electron selection are determined by Monte Carlo, assuming the maximum bias in the acceptance consistent with the measured inefficiencies. Varying the calorimeter energy scales by 5% in the Monte Carlo changes $A_{\rm FB}$ by $< 0.03\%$.

$A_{\rm FB}$ has contributions from background, p_T^Z smearing, and higher order QED and weak processes. We subtract from $A_{\rm FB}$ the contributions from background and p_T^Z smearing, then derive $\sin^2\bar{\theta}_W$ from the corrected $A_{\rm FB}$.

The order α_s QCD diagrams affect the measured asymmetry by smearing the angular distribution for Z^0's with large transverse momentum, p_T^Z. We estimate the size of this effect by convoluting our measured p_T^Z spectrum [9] with a calculation of A_{FB} as a function of p_T^Z [10]. After background and p_T^Z corrections, we find $A_{FB} = (5.3 \pm 5.9(\text{stat}) \pm 0.4(\text{sys}))\%$. The uncertainty on the measured A_{FB} is dominated by statistics.

We make higher order electroweak corrections in order to estimate $\sin^2\bar{\theta}_W$. We integrate the order α^3 QED cross section using a Monte Carlo and a simple detector simulation which accounts for bremsstrahlung [11]. Calculations performed for $e^+e^- \rightarrow q\bar{q}$ [12] are time reversed to obtain results for $q\bar{q} \rightarrow e^+e^-$. After QED corrections we find $\sin^2\bar{\theta}_W = 0.229$. The uncertainty in the QED corrections to $\sin^2\bar{\theta}_W$ is 0.0014, estimated by varying the infrared cutoff. Including the order α^3 weak corrections, we find $\sin^2\bar{\theta}_W = 0.228$. The theoretical uncertainty on the weak calculations is 0.0002.

There is an uncertainty in the relative contributions of u valence quarks, d valence quarks, and sea quarks in the proton, giving an uncertainty on $\sin^2\bar{\theta}_W$ of 0.0004, determined by integrating the cross section with several different parametrizations [7,13]. We use the MRSB parametrization for the final result.

Our final result, $\sin^2\bar{\theta}_W = 0.228^{+0.017}_{-0.015}(\text{stat}) \pm 0.002(\text{sys})$, is in good agreement with the values $\sin^2\bar{\theta}_W = 0.2291 \pm 0.0040$ measured by ALEPH [14], $\sin^2\bar{\theta}_W = 0.2309 \pm 0.0048$ measured by DELPHI [15], and $\sin^2\bar{\theta}_W = 0.230 \pm 0.004$ measured by L3 [16] from the Z^0 mass and leptonic width, and with the value $\sin^2\bar{\theta}_W = 0.233^{+0.007}_{-0.006}$ measured by OPAL [17] from a simultaneous fit to the leptonic cross sections and forward–backward asymmetries.

The parameter $\sin^2\bar{\theta}_W$ is measured from the asymmetry, and $\sin^2\theta_W|_{mass} = 1 - M_W^2/M_Z^2$ [18] from the ratio of the W and Z^0 masses. We use the Standard Model to convert our measurement of $\sin^2\bar{\theta}_W$ from the asymmetry into a measurement of $\sin^2\theta_W|_{mass}$ [19,20]. A plot of $\sin^2\theta_W|_{mass}$ derived from the asymmetry as a function of the top mass is shown by the solid line in Figure 2, assuming a Higgs mass of 250 GeV (the Higgs mass dependence is small); the dashed lines indicate the 1σ experimental uncertainty. Figure

2 also shows the 1σ confidence region derived from recent Z^0 mass measurements [21,22] as well as a direct measurement of $1 - M_W^2/M_Z^2 = 0.232 \pm 0.008$[23] determined from the CDF W and LEP Z^0 masses. A_{FB} is not strongly dependent on the top mass; the top mass dependence in Figure 2 comes from higher order corrections in the Standard Model incurred in the conversion from $\sin^2\bar{\theta}_W$ to $\sin^2\theta_W|_{mass}$.

In summary, we have measured $A_{FB} = (5.3 \pm 5.9(\text{stat}) \pm 0.4(\text{sys}))\%$ after background and QCD corrections, and $\sin^2\bar{\theta}_W = 0.228^{+0.017}_{-0.015}(\text{stat}) \pm 0.002(\text{sys})$ after background and radiative corrections. The systematic uncertainties are summarized in Table 1. Our measurement of $\sin^2\bar{\theta}_W$ is consistent, both without and with order α^3 radiative corrections, with previous measurements of $\sin^2\bar{\theta}_W$ at the Z^0 mass. Our measurement of $\sin^2\theta_W|_{mass}$ from the asymmetry is consistent with measurements of $\sin^2\theta_W|_{mass}$ from the W and Z^0 mass ratio over a broad range of top quark masses.

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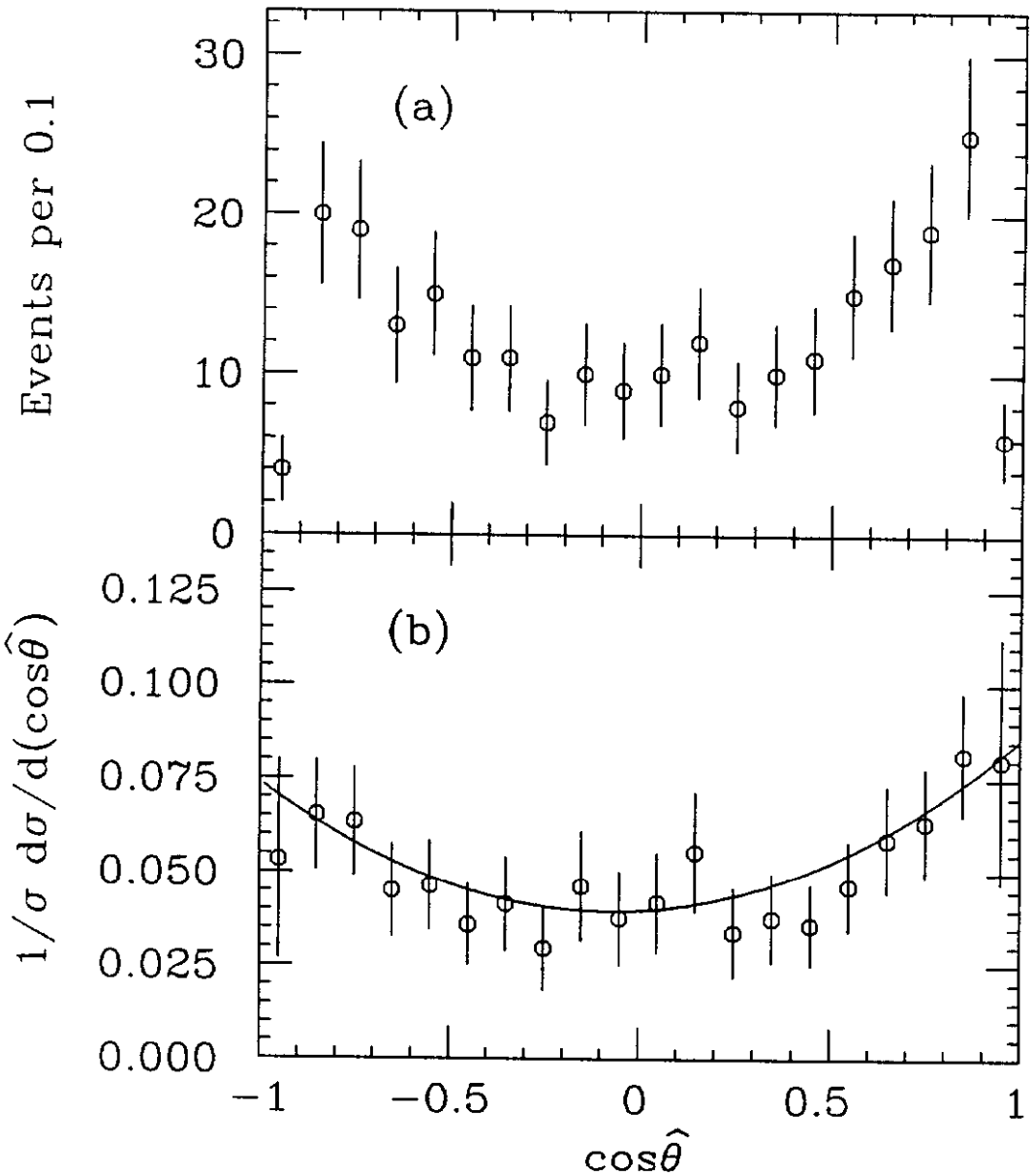
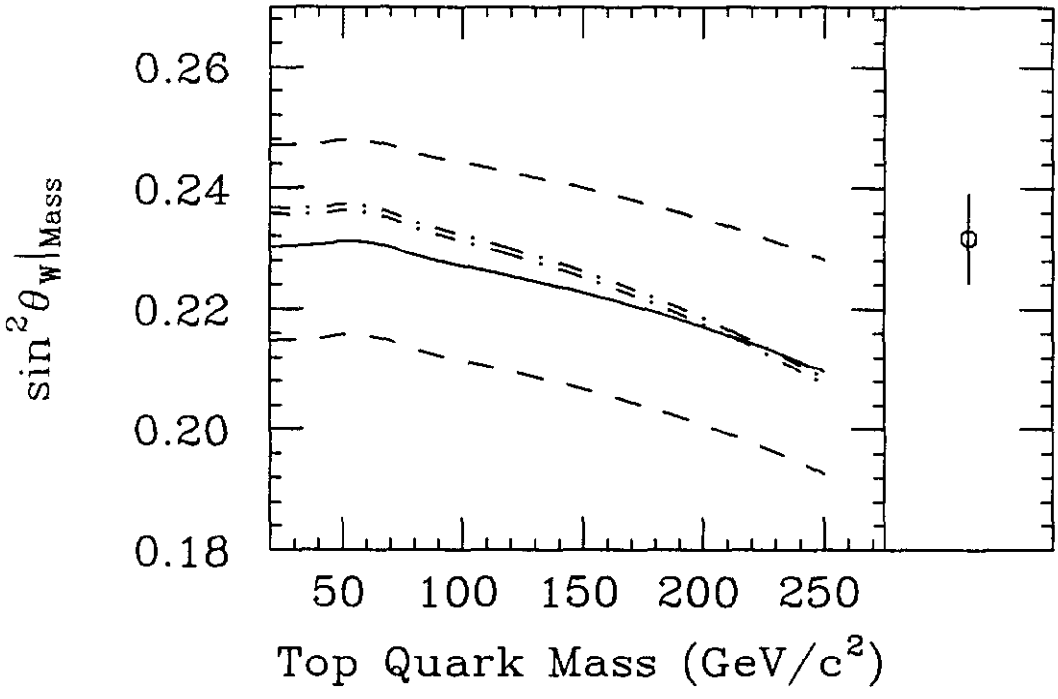
Figure 1: Angular distribution of electrons (a) before and (b) after acceptance corrections. The solid line is the result of the likelihood fit.

Figure 2: The solid line shows the central value of $\sin^2\theta_W|_{mass}$ derived from the asymmetry as a function of the top quark mass; the dashed lines indicate the 1σ experimental uncertainty. The dot-dashed lines show the 1σ uncertainty on $\sin^2\theta_W|_{mass}$ determined from Z^0 mass measurements. At right is the CDF value from $1 - M_W^2/M_Z^2$ [23] .


(a)
(b)
Events per 0.1
$1/\sigma\ d\sigma/d(\cos\hat{\theta})$
$\cos\hat{\theta}$
30
20
10
0
0.125
0.100
0.075
0.050
0.025
0.000
−1
−0.5
0
0.5
1


0.26
0.24
0.22
0.20
0.18
$\sin^2\theta_W|_{Mass}$
50
100
150
200
250
Top Quark Mass (GeV/c^2)